



PhysicsByAaryan

TIFR Physics 2024

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Atomic and Molecular Physics

Q1. [TIFR_2024_C_Q11]

Year 2024 · Atomic and Molecular Physics · Effects in atomic physics · Only PhD · 5 marks

TIFR GS	2024	Section C
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The Hamiltonian for a Helium atom is given as $H = H_0 + H_1$, where

$$H_0 = \frac{(p_1^2 + p_2^2)}{2\mu} - \frac{2e^2}{4\pi\epsilon_0 r_1} - \frac{2e^2}{4\pi\epsilon_0 r_2}$$

and

$$H_1 = \frac{e^2}{4\pi\epsilon_0 r_{12}}$$

where μ is the reduced mass of the electron, r_1 and r_2 are the distance of the electrons from the nucleus, and r_{12} is the distance between the two electrons. The value of the first ionization potential of the Helium atom is 24.6 eV .

What is the correction due to H_1 to the ground state energy of the Helium atom, compared to H_0 ?

- (a) 29.8 eV
- (b) -29.8 eV
- (c) 84.2 eV
- (d) -2.6 eV

Classical Mechanics

Q2. [TIFR_2024_A_Q12]

Year 2024 · Classical Mechanics · Central Forces, Gravitation and Universe · Both int. phd and phd · 3 marks

TIFR GS	2024	Section A
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In an infinite fluid of density ρ there are two spherical gas bubbles of radii r_1 and r_2 respectively. The gas has density $\rho_g < \rho$. The centres of the bubbles are separated by a distance $R \gg r_1, r_2$. If the space has no other forces than gravity, the bubbles will:

(a) Move towards each other due to an attractive gravitational force

$$F = G(\rho - \rho_g)^2 \left(\frac{4\pi}{3}\right)^2 \frac{r_1^3 r_2^3}{R^2}$$

(b) Move towards each other due to an attractive gravitational force

$$F = G(\rho - \rho_g)^2 \left(\frac{4\pi}{3}\right)^2 \frac{r_1^3 r_2^3}{R^2}$$

(c) Move away from each other due to a repulsive gravitational force

$$F = G(\rho - \rho_g)^2 \left(\frac{4\pi}{3}\right)^2 \frac{r_1^3 r_2^3}{R^2}$$

(d) Move away from each other due to a repulsive gravitational force

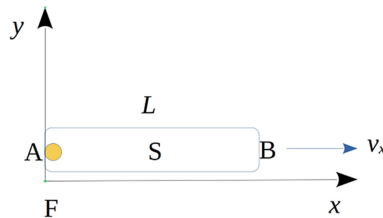
$$F = G(\rho - \rho_g)^2 \left(\frac{4\pi}{3}\right)^2 \frac{r_1^3 r_2^3}{R^2}$$

Q3. [TIFR_2024_A_Q22]

Year 2024 · Classical Mechanics · Special Theory of Relativity · Both int. phd and phd · 3 marks

TIFR GS	2024	Section A
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Consider a spaceship S of length L is moving relativistically in the x direction with a speed v_x relative to an inertial reference frame F as shown in the figure.



In S, a light bulb is placed at the left end (point A) and a detector is placed at the right end (point B). What is the time taken for light to travel from A to B in the reference frame F?

(a) $\frac{L}{c} \sqrt{\frac{1+v_x/c}{1-v_x/c}}$

(b) $\frac{L}{c} \sqrt{1 - \frac{v_x^2}{c^2}}$

(c) $\frac{L}{c} \sqrt{\frac{1-v_x/c}{1+v_x/c}}$

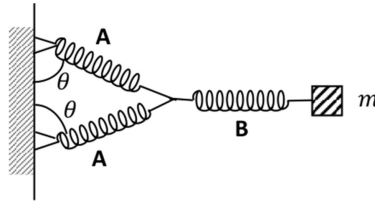
(d) $\frac{L}{c} \frac{1}{\sqrt{1-v_x^2/c^2}}$

Q4. [TIFR_2024_A_Q4]

Year 2024 · Classical Mechanics · Oscillations · Both int. phd and phd · 3 marks

TIFR GS	2024	Section A
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Consider a mass m connected to a network of massless springs shown in the figure below.



The spring constant of spring A is k_A , and that of spring B is k_B . The springs are shown in a relaxed position, and the angle θ in this position is $\pi/3$. The mass is displaced horizontally by a small distance. What is the angular frequency of small oscillations of m ? (Ignore gravity and friction.)

- (a) $\sqrt{(3k_A k_B)/[m(2k_B + 3k_A)]}$
 (b) $\sqrt{(k_A k_B)/[m(k_B + k_A)]}$
 (c) $\sqrt{(2k_A k_B)/[m(k_B + 2k_A)]}$
 (d) $\sqrt{(\sqrt{3}k_A k_B)/[m(k_B + \sqrt{3}k_A)]}$

Q5. [TIFR_2024_A_Q5]

Year 2024 · Classical Mechanics · Basic Mechanics · Both int. phd and phd · 3 marks

TIFR GS	2024	Section A
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Consider an object falling in air. In addition to gravity, it experiences an air resistance force, R , given by $R = bv$, where v is the speed and b is a constant. If the object is dropped from rest ($v = 0$ at $t = 0$), the distance traversed by the object at $t = m/b$ is:

- (a) $\left(\frac{m^2 g}{b^2}\right) \left(\frac{1}{e}\right)$
 (b) $\left(\frac{m^2 g}{b^2}\right) \left(1 - \frac{1}{e}\right)$
 (c) $\left(\frac{m^2 g}{b^2}\right) (e - 1)$
 (d) $\left(\frac{m^2 g}{b^2}\right) \left(2 - \frac{1}{e}\right)$

Q6. [TIFR_2024_A_Q6]

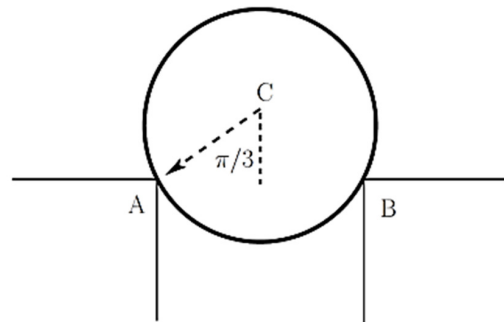
Year 2024 · Classical Mechanics · Basic Mechanics · Both int. phd and phd · 3 marks

TIFR GS	2024	Section A
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A frictionless disk of mass m is balanced at rest on the edges of two platforms at points A and B that are at equal height as shown below. The angle made by the line joining the centre to point A (line CA) with the vertical is $\pi/3$.

What is the magnitude of the force exerted by point A on the disk?

- (a) mg
- (b) $\frac{mg}{2}$
- (c) $\frac{mg}{\sqrt{3}}$
- (d) $\frac{mg\sqrt{3}}{2}$

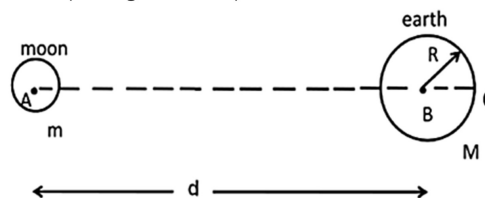


Q7. [TIFR_2024_B_Q12]

Year 2024 · Classical Mechanics · Central Forces, Gravitation and Universe · Only int. Phd · 5 marks

TIFR GS	2024	Section B
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A tidal force is exerted on the oceans by the Moon. This can be estimated by the differential acceleration (Δg) which is the difference between the gravitational acceleration at B and C due to the moon (see figure below).



If R and M are the radius and mass of Earth, d the distance of separation of the centre of Earth and the moon, and m the mass of moon, which of the following answers is closest to the magnitude of Δg ?

- (a) $\frac{2GmR}{d^3}$
- (b) $\frac{4GmR}{d^3}$
- (c) $\frac{GmR}{2d^3}$
- (d) $\frac{GmR^2}{d^4}$

Q8. [TIFR_2024_B_Q14]

Year 2024 · Classical Mechanics · Special Theory of Relativity · Only int. Phd · 5 marks

TIFR GS	2024	Section B
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A massive particle moving at a speed of $4c/5$ collides with an identical particle at rest. What would be the speed of the second particle in the center-of-mass frame after the collision?

- (a) $c/2$
- (b) $2c/5$
- (c) $c/\sqrt{2}$
- (d) $2\sqrt{2}c/5$

Q9. [TIFR_2024_B_Q2]

Year 2024 · Classical Mechanics · Central Forces, Gravitation and Universe · Only int. Phd · 5 marks

TIFR GS	2024	Section B
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Consider a particle of mass m orbiting around a central potential $V(r) = -\frac{a}{r} - \frac{b}{r^3}$ with $a, b > 0$. What is the smallest angular momentum it must have to be in a stable orbit?

- (a) $(12abm^2)^{1/4}$
- (b) $(4abm^2)^{1/4}$
- (c) $(3abm^2)^{1/4}$
- (d) $(6abm^2)^{1/4}$

Q10. [TIFR_2024_B_Q3]

Year 2024 · Classical Mechanics · Lagrangian and Hamiltonian · Only int. Phd · 5 marks

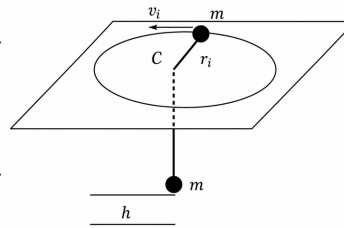
TIFR GS	2024	Section B
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Two equal masses m are connected with a massless string. The first mass is initially set in a uniform circular motion with speed v_i at a radius r_i on top of a table while the second mass hangs vertically on the string which passes through a hole in the centre of the table (C), as shown in the figure below.

The system is released with this initial configuration and the second mass starts falling. What is the net speed of the first mass when the second mass has fallen a height h (smaller than r_i)?

(Assume that there is no friction and that the string always remains tight.)

- (a) $\sqrt{gh + \frac{1}{2}v_i^2 \left[1 + \frac{r_i^2}{(r_i-h)^2}\right]}$
- (b) $\sqrt{gh + \frac{1}{2}v_i^2 \left[1 + \frac{r_i}{(r_i-h)}\right]}$
- (c) $\sqrt{gh + \frac{1}{2}v_i^2 \left[1 + \frac{(r_i-h)^2}{r_i^2}\right]}$
- (d) $\sqrt{gh + \frac{1}{2}v_i^2 \left[1 + \frac{(r_i-h)}{r_i}\right]}$



Q11. [TIFR_2024_C_Q13]

Year 2024 · Classical Mechanics · Central Forces, Gravitation and Universe · Only PhD · 5 marks

TIFR GS	2024	Section C
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Consider a universe that always expands with a scale factor a that increases with time as $a(t) = Ct^{2/3}$ where C is a constant. Its expansion rate at time t is defined by the Hubble parameter

$$H(t) = \frac{1}{a(t)} \frac{da(t)}{dt}$$

The current value of $H(t)$ in the universe is given by $H_0 = 975 \text{ km s}^{-1} \text{ Mpc}^{-1}$ where $1 \text{ Mpc} = 3.1 \times 10^{22} \text{ m}$. What is the approximate age of this universe?

- (a) 10^9 years
- (b) 10^7 years
- (c) 10^{11} years
- (d) 10^{13} years

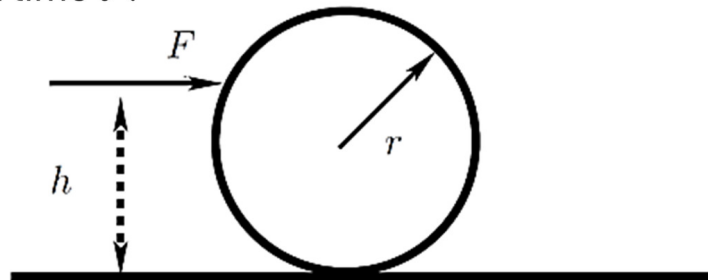
Q12. [TIFR_2024_C_Q3]

Year 2024 · Classical Mechanics · Rotational Motion · Only PhD · 5 marks

TIFR GS	2024	Section C
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A horizontal constant force F is applied on a uniform disc placed on a horizontal surface. The mass of the disc is m , and the radius is r . The point of application of F is at a height $h (< 2r)$ from the surface. The disc starts from rest at $t = 0$ and rolls without slipping. What is the speed of the centre of the disc at time t ?

- (a) $\frac{2Fht}{3mr}$
- (b) $\frac{Ft}{m}$
- (c) $\frac{2Ft}{3m}$
- (d) $\frac{3Fht}{2mr}$

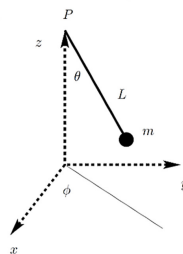


Q13. [TIFR_2024_C_Q4]

Year 2024 · Classical Mechanics · Lagrangian and Hamiltonian · Only PhD · 5 marks

TIFR GS	2024	Section C
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A particle of mass m is attached to a massless string of length L . The other end of the string is fixed at a point P as shown in the figure.



m moves under gravity and the tension of the string. The motion of the string is described using the generalized coordinates θ and ϕ which change with time. θ is the polar angle made by the string with the vertical and ϕ is the azimuthal angle made by the projection of the string on the xy plane. The conjugate momenta to the variables (θ, ϕ) are (p_θ, p_ϕ) , respectively.

Assuming that the string is tight throughout the motion, the Hamiltonian for the system is given by:

- (a) $\frac{1}{2m} [p_\theta^2 + p_\phi^2 \operatorname{cosec}^2 \theta] + 2mgL \sin^2 \left(\frac{\theta}{2} \right)$
- (b) $\frac{1}{2m} [p_\theta^2 + p_\phi^2 \operatorname{cosec}^2 \theta] - 2mgL \sin^2 \left(\frac{\theta}{2} \right)$
- (c) $\frac{1}{2m} [p_\theta^2 + p_\phi^2 \sin^2 \theta] + 2mgL \sin^2 \left(\frac{\theta}{2} \right)$
- (d) $\frac{1}{2m} [p_\theta^2 + p_\phi^2 \sin^2 \theta] - 2mgL \sin^2 \left(\frac{\theta}{2} \right)$

Electromagnetism

Q14. [TIFR_2024_A_Q10]

Year 2024 · Electromagnetism · Electrostatics · Both int. phd and phd · 3 marks

TIFR GS	2024	Section A
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A thin spherical shell of radius R has a constant surface charge density σ . This shell is cut symmetrically into two pieces. What is the electrostatic force between the two halves?

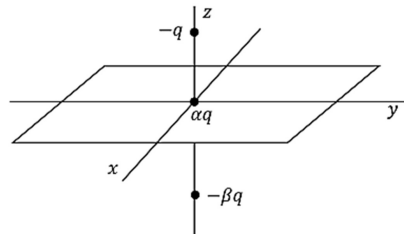
- (a) $\frac{\pi \sigma^2 R^2}{2 \epsilon_0}$
- (b) $\frac{\pi \sigma^2 R^2}{4 \epsilon_0}$
- (c) $\pi \frac{\sigma^2 R^2}{\epsilon_0}$
- (d) $2\pi \frac{\sigma^2 R^2}{\epsilon_0}$

Q15. [TIFR_2024_A_Q11]

Year 2024 · Electromagnetism · Multipole Expansion · Both int. phd and phd · 3 marks

TIFR GS	2024	Section A
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Consider a system of three electric charges: (i) a charge $-q$ placed at the point $(x, y, z) = (0, 0, d)$, (ii) a charge $+\alpha q$ placed at the origin and (iii) a charge $-\beta q$ placed at the point $(x, y, z) = (0, 0, -d)$.



The values of α and β are such that the monopole and dipole terms vanish in the multipole expansion of the electrostatic potential.

What is the quadrupole term of the potential at a point $(x, y, 0)$?

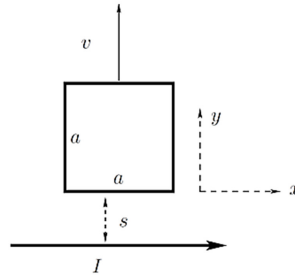
- (a) $\frac{q}{4\pi\epsilon_0} \frac{d^2}{(x^2+y^2)^{3/2}}$
- (b) $\frac{q}{2\pi\epsilon_0} \frac{d^2}{(x^2+y^2)^{3/2}}$
- (c) 0
- (d) $\frac{q}{4\pi\epsilon_0} \frac{1}{(x^2+y^2)^{1/2}}$

Q16. [TIFR_2024_B_Q6]

Year 2024 · Electromagnetism · Electrodynamics · Only int. Phd · 5 marks

TIFR GS	2024	Section B
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A conducting square loop of wire (side a) lies on a table, at a distance s from an infinite straight wire as shown in the figure.



The infinite wire carries a current I in the x direction as shown. If one now pulls the loop directly away from the wire in the y direction at a constant speed v , what is the generated EMF in the loop? In what direction (clockwise or counterclockwise) does the current flow in the loop?

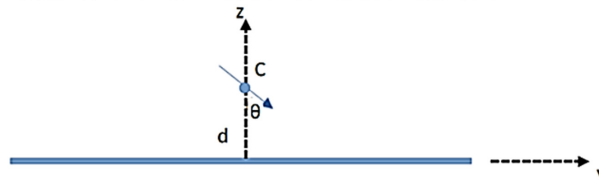
- (a) $\frac{a^2 v I \mu_0}{2\pi(as+s^2)}$, anticlockwise
- (b) $\frac{a^2 v I \mu_0}{2\pi(as+s^2)}$, clockwise
- (c) $\frac{av I \mu_0}{2\pi(a+s)}$, anticlockwise
- (d) $\frac{av I \mu_0}{2\pi(a+s)}$, clockwise

Q17. [TIFR_2024_B_Q7]

Year 2024 · Electromagnetism · Electrostatics · Only int. Phd · 5 marks

TIFR GS	2024	Section B
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Consider an electric dipole of strength p placed near a grounded infinite conducting sheet in the xy plane at a distance d from it in the z direction as shown below.



The centre of the dipole (C) is fixed to a pivot but the dipole is free to rotate about the x axis (coming out of the page). What is the magnitude of the torque on the dipole when the angle between the dipole and the positive z axis is $(\pi - \theta)$ as shown?

- (a) $\tau = \frac{p^2}{(64\pi\epsilon_0 d^3)} \sin(2\theta)$
- (b) $\tau = \frac{p^2}{(16\pi\epsilon_0 d^3)} \cos(2\theta)$
- (c) $\tau = \frac{p^2}{(64\pi\epsilon_0 d^3)} \cos(\theta)$
- (d) $\tau = \frac{p^2}{(16\pi\epsilon_0 d^3)} \sin(\theta)$

Q20. [TIFR_2024_A_Q17]

Year 2024 · Electronics · Logic Gates · Both int. phd and phd · 3 marks

TIFR GS	2024	Section A
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The minimum number of two input NAND gates required to obtain the output $Y = \bar{A}B + \bar{C}$ from three inputs A, B and C is:

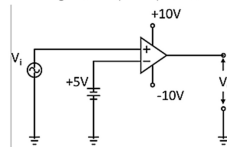
- (a) 3
- (b) 7
- (c) 4
- (d) 6

Q21. [TIFR_2024_B_Q10]

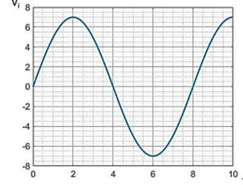
Year 2024 · Electronics · OPAMP · Only int. Phd · 5 marks

TIFR GS	2024	Section B
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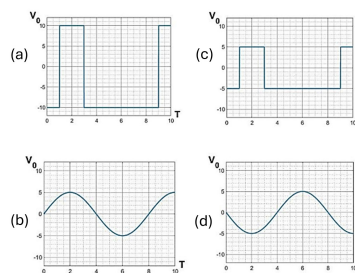
In the following ideal Op-Amp circuit



if the input voltage V_i is



The output waveform would be



Experimental Physics

Q22. [TIFR_2024_A_Q18]

Year 2024 · Experimental Physics · Data Analysis · Both int. phd and phd · 3 marks

TIFR GS	2024	Section A
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A student measures the radioactive decay of a material with a half-life of 13,000 years with a Geiger counter. In the laboratory notebook, the student records the following number of decays every 10 seconds:

158,146,145,163,154,163,160,160,152,157,154,
156,149,168,152

The teacher suspects that the experiment was not done properly and the student created the numbers manually.

Why would the teacher have such a suspicion?

- (a) The variance is much less than the mean, unlike what is expected for a Poisson distribution.
- (b) The standard deviation is much less than the variance, as expected for a Poisson distribution.
- (c) The median is less than the mean, unlike what is expected for a Poisson distribution.
- (d) The median is greater than the mean, as expected for a Poisson distribution.

Q23. [TIFR_2024_B_Q11]

Year 2024 · Experimental Physics · Instruments · Only int. Phd · 5 marks

TIFR GS	2024	Section B
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A mass spectrometer consists of a parallel plate capacitor with plates A and B that accelerates ions through an electric potential V , which is followed by a box carrying a uniform magnetic field B of magnitude 0.2 Tesla (coming out of the page as shown).

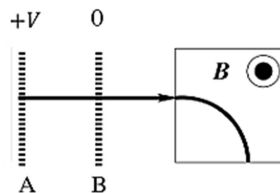
This setup is used to separate two isotopes of Uranium:

$$^{235}\text{U} (\text{mass} = 3.93 \times 10^{-25} \text{ kg})$$

$$^{238}\text{U} (\text{mass} = 3.98 \times 10^{-25} \text{ kg})$$

Singly charged ions (charge $+e$) of the two isotopes are created at the plate A and pass without energy loss through plate B into the box. In order to separate the isotopes, their radii of curvature in the box must differ by 2 mm. What is the approximate V through which the ions must be accelerated in order to achieve this?

- (a) 800 Volts
- (b) 8000 Volts
- (c) 80 Volts
- (d) 8 Volts



Q24. [TIFR_2024_C_Q10]

Year 2024 · Experimental Physics · Data Analysis · Only PhD · 5 marks

TIFR GS	2024	Section C
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A particular counting system has an average background rate of 50 counts /min. A decaying radioisotope source was introduced and the total 168 counts were measured in one minute. After a delay of 24 hrs , the system measured total 91 counts in one minute. If these measurements were used for determining the half-life (τ) of the source and if the average background rate, and the time have no errors, the % error ($100 \times \sigma_{\tau}/\tau$) in the calculated half-life value due to counting statistics would be:

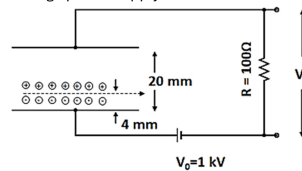
- (a) 24.3%
- (b) 21.2%
- (c) 25.7%
- (d) 18.2%

Q25. [TIFR_2024_C_Q9]

Year 2024 · Experimental Physics · Instruments · Only PhD · 5 marks

TIFR GS	2024	Section C
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Consider a charge particle detection chamber as shown in the figure below. The chamber is made of a set of parallel plates separated by 20 mm distance and connected to the external resistance ($R=100\ \Omega$) as shown in the figure along with the high voltage power supply of 1 kV .



The chamber is filled with Argon (Ar) gas (ionization energy 16 eV). If a charged particle passes through the chamber and loses sufficient energy, it ionizes the Ar atoms and generates a small voltage pulse across the resistance R .

In an experiment, an alpha particle of energy 5.5 MeV enters the chamber at a distance of 4 mm from the bottom plate, as shown, generating ion-electron pairs. If the effective capacitance of the chamber is 100 pF , the measured voltage pulse shape would be best described as:

- (a) A sharp voltage pulse followed by a very weak broad pulse
- (b) Two sharp voltage pulses of equal magnitude and opposite signs
- (c) Two sharp voltage pulses of the same magnitude and sign
- (d) No voltage pulse would be generated as both electrons and ions will neutralise the charge collected by the capacitor

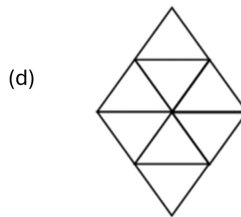
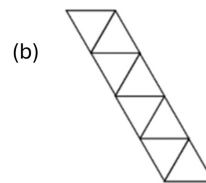
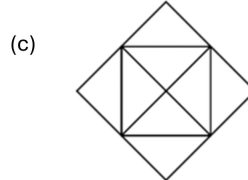
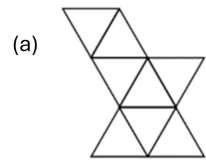
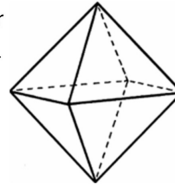
Geometry

Q26. [TIFR_2024_A_Q1]

Year 2024 · Geometry · Geometry · Both int. phd and phd · 3 marks

TIFR GS	2024	Section A
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Which of the following sheets of paper can be turned into a regular octahedron (a three-dimensional regular polyhedron with eight triangular faces, as shown on the right) by folding along the marked lines?

**Mathematical Physics****Q27.** [TIFR_2024_A_Q2]

Year 2024 · Mathematical Physics · Vector Analysis · Both int. phd and phd · 3 marks

TIFR GS	2024	Section A
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A surface is given by

$$2x^3z + 4y^2z + 3z^2 = 81$$

Which of the following is a vector tangential to it at the point on the surface with coordinates

$(x, y, z) = (1, 2, 3)$?

(a) $2\hat{i} - 3\hat{j} + 3\hat{k}$

(b) $18\hat{i} + 48\hat{j} + 36\hat{k}$

(c) $-3\hat{i} + 2\hat{j} + 6\hat{k}$

(d) $-3\hat{i} - 2\hat{j} + 6\hat{k}$

Q28. [TIFR_2024_A_Q3]

Year 2024 · Mathematical Physics · Differential Equations · Both int. phd and phd · 3 marks

TIFR GS	2024	Section A
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Consider the following differential equations:

$$\frac{dx}{dt} = ay(t), \frac{dy}{dt} = a$$

where a is a positive constant. The solutions to these equations define a family of curves in the x, y plane. What are these curves?

- (a) Parabolas
- (b) Circles
- (c) Hyperbolas
- (d) Ellipses

Q29. [TIFR_2024_B_Q1]

Year 2024 · Mathematical Physics · Limits, Continuity and Differentiation · Only int. Phd · 5 marks

TIFR GS	2024	Section B
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The following series

$$S = \sum_{n=1}^{\infty} (-1)^{1+n} \frac{1}{n2^{4n}}$$

has the sum

- (a) $S = \ln\left(\frac{17}{16}\right)$
- (b) $S = \sqrt{\frac{17}{16}}$
- (c) S is not convergent
- (d) $S = \frac{1}{1 + \sqrt{\frac{1}{16}}}$

Q30. [TIFR_2024_C_Q1]

Year 2024 · Mathematical Physics · Matrices · Only PhD · 5 marks

TIFR GS	2024	Section C
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Consider the following matrix

$$M = \begin{pmatrix} 1 & 5 & -7 & 1 \\ 1 & 0 & 2 & 2 \\ 9 & -1 & 3 & 1 \\ 9 & 6 & -7 & -4 \end{pmatrix}$$

What is $\det e^M$?

- (a) 1
- (b) e
- (c) e^{1210}
- (d) e^{-1210}

Q31. [TIFR_2024_C_Q2]

Year 2024 · Mathematical Physics · Fourier and Laplace Analysis · Only PhD · 5 marks

TIFR GS	2024	Section C
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Let

$$F(\lambda) = \int_{-\infty}^{+\infty} dx e^{\lambda x - x^2}$$

If the Taylor series expansion of $F(\lambda)$ around $\lambda = 0$ is

$$F(\lambda) = F_0 + F_1\lambda + F_2\lambda^2 + \dots$$

then the value of F_2 is

(You might find the following integral useful:

$$\int_{-\infty}^{+\infty} dx e^{-\alpha x^2} = \sqrt{\frac{\pi}{\alpha}} \text{ for } \alpha > 0)$$

- (a) $\sqrt{\pi}/4$
- (b) $\sqrt{\pi}/8$
- (c) $\sqrt{\pi}/2$
- (d) $\sqrt{\pi}$

Modern Physics

Q32. [TIFR_2024_A_Q23]

Year 2024 · Modern Physics · Light Matter interaction · Both int. phd and phd · 3 marks

TIFR GS	2024	Section A
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A beam of neutrons is incident normally upon a thick sheet of Cadmium. The mass density of Cadmium is $\rho = 8.6 \text{ g cm}^{-3}$. The absorption cross-section of neutrons on Cadmium nuclei is $2.5 \times 10^{-20} \text{ cm}^2$. The atomic weight of Cadmium is known to be 112.40 g/mol. You may take $N_A = 6.02 \times 10^{23}$.

At what depth is the intensity of the beam reduced by a factor $\frac{1}{e}$?

- (a) $9 \mu \text{ m}$
- (b) 9 fm
- (c) 9 nm
- (d) 900 fm

Nuclear and Particle Physics**Q33.** [TIFR_2024_A_Q21]

Year 2024 · Nuclear and Particle Physics · Radioactivity · Both int. phd and phd · 3 marks

TIFR GS	2024	Section A
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The ionization potential of the H atom is 13.598 eV .
If the mass of a proton is $1.673 \times 10^{-27} \text{ kg}$, the mass of an electron is $9.109 \times 10^{-31} \text{ kg}$ and the mass of the D nucleus is $3.344 \times 10^{-27} \text{ kg}$, the ionization potential of the D atom is given by:

- (a) 13.602 eV
- (b) 13.594 eV
- (c) 13.598 eV
- (d) 27.188 eV

Q34. [TIFR_2024_C_Q12]

Year 2024 · Nuclear and Particle Physics · Shell Model · Only PhD · 5 marks

TIFR GS	2024	Section C
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Oxygen (O) nuclei ($Z = 8$) can be approximated as non-interacting protons and neutrons filling up orbitals in the following order.

$$1s_{1/2}, 1p_{3/2}, 1p_{1/2}, 1d_{5/2}, 2s_{1/2}, 1d_{3/2}, \dots$$

where the subscript specifies the J quantum number. Given the binding energy of O ($A = 15$) is 111.96 MeV, O ($A = 16$) is 127.62 MeV, and O ($A = 17$) is 131.76 MeV, what is the difference between the energies of the $1p_{1/2}$ and the $1d_{5/2}$ orbitals?

- (a) 11.52 MeV
- (b) 15.66 MeV
- (c) 4.14 MeV
- (d) 19.81 MeV

Q35. [TIFR_2024_C_Q15]

Year 2024 · Nuclear and Particle Physics · Radioactivity · Only PhD · 5 marks

TIFR GS	2024	Section C
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Consider an unstable bound state B of a proton (p) with an antiproton (\bar{p}), which is in the S-state ($\ell = 0$) in the spin-singlet configuration. When this state B decays, which of the following final states will NOT be possible?

- (a) $\gamma + \gamma + \gamma$
- (b) $\mu^+ + \mu^- + \gamma$
- (c) $\gamma + \gamma$
- (d) $e^+ + e^- + \gamma$

Optics

Q36. [TIFR_2024_A_Q19]

Year 2024 · Optics · Polarization · Both int. phd and phd · 3 marks

TIFR GS	2024	Section A
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Unpolarised light of intensity 200 W/m^2 is incident on a set of two perfect polarisers arranged one behind the other. The first polariser has its transmission axis at $+55^\circ$ with respect to the vertical and the second polariser has its transmission axis at $+100^\circ$ with respect to the vertical. What is the intensity of the transmitted light?

- (a) 50 W/m^2
- (b) 100 W/m^2
- (c) 1.98 W/m^2
- (d) 3.01 W/m^2

Q37. [TIFR_2024_A_Q20]

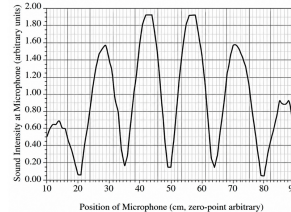
Year 2024 · Optics · Interference · Both int. phd and phd · 3 marks

TIFR GS	2024	Section A
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Two small loudspeakers A and B, separated by 15 cm, were pointed toward a small microphone M at a distance 1.5 m away from the centre of the line AB, in the perpendicular direction as shown in the sketch below.



The following sound intensity pattern was observed as a function of the position of the microphone as it is moved parallel to AB.



The dips in the signal were repeated at the interval of 14.5 cm. The speed of sound in the experiment's background condition is 343 m/s. What can we conclude from this information?

- (a) The two loudspeakers are vibrating at frequency 23.65 kHz and they are out of phase.
- (b) The two loudspeakers are vibrating at frequency 23.65 kHz and they are in phase.
- (c) The two loudspeakers are vibrating at frequency 47.3 kHz and they are in phase.
- (d) The two loudspeakers are vibrating at frequency 47.3 kHz and they are out of phase.

Q38. [TIFR_2024_B_Q13]

Year 2024 · Optics · Polarization · Only int. Phd · 5 marks

TIFR GS	2024	Section B
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Incident unpolarized light is reflected from a glass ($n_g = 1.65$) plate immersed in ethyl alcohol ($n_a = 1.36$) and this reflection is found to be completely linearly polarised. Find the angle at which the incident light would be transmitted through the plate.

- (a) 39.5°
- (b) 31.6°
- (c) 50.5°
- (d) 69.3°

Quantum Mechanics**Q39.** [TIFR_2024_A_Q24]

Year 2024 · Quantum Mechanics · Potential Well · Both int. phd and phd · 3 marks

TIFR GS	2024	Section A
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An electron confined in a two-dimensional square box, is in the ground state. The length of the side of this square is unknown, but it is seen that the electron jumps to the first excited energy state by absorbing electromagnetic radiation of wavelength 4,040 nm . What is the length of one side of the square well?

- (a) 1.91 nm
- (b) 1.68 nm
- (c) 2.55 nm
- (d) 3.82 nm

Q40. [TIFR_2024_A_Q7]

Year 2024 · Quantum Mechanics · quantum Harmonic Oscillator · Both int. phd and phd · 3 marks

TIFR GS	2024	Section A
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Consider a particle of mass m moving in a one-dimensional potential of the form

$$V(x) = \begin{cases} \frac{1}{2}kx^2 & \text{for } x > 0 \\ \infty & \text{for } x \leq 0 \end{cases}$$

In a quantum mechanical treatment, what is the ground state energy of the particle?

- (a) $\frac{3}{2}\hbar\sqrt{\frac{k}{m}}$
 (b) $\frac{1}{2}\hbar\sqrt{\frac{k}{m}}$
 (c) $\hbar\sqrt{\frac{k}{m}}$
 (d) $\frac{5}{2}\hbar\sqrt{\frac{k}{m}}$

Q41. [TIFR_2024_A_Q8]

Year 2024 · Quantum Mechanics · quantum Harmonic Oscillator · Both int. phd and phd · 3 marks

TIFR GS	2024	Section A
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The un-normalized energy eigenfunction of a one-dimensional simple quantum harmonic oscillator in dimensionless units ($m = \hbar = \omega = 1$) is

$$\psi_a(x) = (2x^3 - 3x)e^{-x^2/2}$$

Which of the following are two other (un-normalized) eigenfunctions which are closest in energy to ψ_a ?

- (a) $(2x^2 - 1)e^{-x^2/2}; (4x^4 - 12x^2 + 3)e^{-x^2/2}$
 (b) $e^{-x^2/2}; (2x^2 - 1)e^{-x^2/2}$
 (c) $xe^{-x^2/2}; (4x^5 - 20x^3 + 15x)e^{-x^2/2}$
 (d) $(2x^2 - 1)e^{-x^2/2}; (4x^5 + 20x^3 + 15x)e^{-x^2/2}$

Q42. [TIFR_2024_A_Q9]

Year 2024 · Quantum Mechanics · Angular Momentum and Hydrogen atom · Both int. phd and phd · 3 marks

TIFR GS	2024	Section A
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A quantum-mechanical state of a particle, with Cartesian coordinates x, y and z , is described by the normalized wave function

$$\psi(x, y, z) = \frac{\alpha^{5/2}}{\sqrt{\pi}} z e^{-\alpha\sqrt{x^2+y^2+z^2}}$$

For this state what are the angular quantum number ℓ , L^2 and L_z respectively?

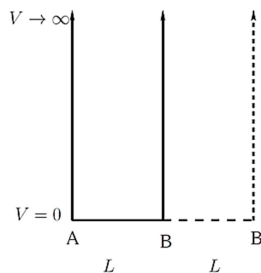
- (a) 1; $2\hbar^2$; 0
- (b) 0; 0; 0
- (c) 1; $2\hbar^2$; \hbar
- (d) 2; $6\hbar^2$; 0

Q43. [TIFR_2024_B_Q4]

Year 2024 · Quantum Mechanics · Basic Quantum Mechanics · Only int. Phd · 5 marks

TIFR GS	2024	Section B
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Consider a particle of mass m moving in an infinite one-dimensional potential well of length L between points A and B. In a quantum-mechanical treatment, the particle is in the ground state with an energy E_g .



The wall at B is suddenly shifted to B' where AB' has length $2L$. If we measure the energy again, what is the most probable result?

- (a) E_g
- (b) $E_g/4$
- (c) $4E_g$
- (d) $9E_g/4$

Q44. [TIFR_2024_B_Q5]

Year 2024 · Quantum Mechanics · Basic Quantum Mechanics · Only int. Phd · 5 marks

TIFR GS	2024	Section B
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A particle of mass m is subjected to a force $\vec{F}(\vec{r})$ such that the wavefunction $\phi(\vec{p}, t)$ satisfies the momentum-space Schrödinger equation

$$\left(\frac{\vec{p}^2}{2m} - a\vec{\nabla}_p^2\right)\phi(\vec{p}, t) = i\hbar\frac{\partial}{\partial t}\phi(\vec{p}, t)$$

where a is a real constant and

$$\vec{\nabla}_p^2 = \frac{\partial^2}{\partial p_x^2} + \frac{\partial^2}{\partial p_y^2} + \frac{\partial^2}{\partial p_z^2}$$

It follows that $\vec{F}(\vec{r}) =$

- (a) $-\frac{2a}{\hbar^2}\vec{r}$
- (b) $\frac{2a}{\hbar^2}\vec{r}$
- (c) $-a\hbar^2\frac{\vec{r}}{r^3}$
- (d) $a\hbar^2\frac{\vec{r}}{r^3}$

Q45. [TIFR_2024_C_Q5]

Year 2024 · Quantum Mechanics · Basic Quantum Mechanics · Only PhD · 5 marks

TIFR GS	2024	Section C
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Consider \hat{x} and \hat{p}_x as the quantum mechanical position and linear momentum operators with eigenstates $|x\rangle$ and $|p_x\rangle$ and eigenvalues x and p_x , respectively.

The eigenvalue of \hat{x} acting on the state

$$|\psi\rangle = e^{i\hat{p}_x a/2\hbar}|x\rangle$$

is

- (a) $x + \frac{a}{2}$
- (b) $x - \frac{a}{2}$
- (c) $x + a$
- (d) $x - a$

Q46. [TIFR_2024_C_Q6]

Year 2024 · Quantum Mechanics · Basic Quantum Mechanics · Only PhD · 5 marks

TIFR GS	2024	Section C
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A particle of mass m moving in 1 dimension has the wavefunction

$$\psi(x) = \frac{1}{\pi^{1/4}\sqrt{a}} e^{ipx/\hbar} e^{-x^2/2a^2}$$

Its average kinetic energy is given by

(You might find the following integral useful:

$$\int_{-\infty}^{+\infty} dx e^{-\alpha x^2} = \sqrt{\frac{\pi}{\alpha}} \text{ for } \alpha > 0)$$

- (a) $\frac{p^2}{2m} + \frac{\hbar^2}{4a^2m}$
 (b) $\frac{\left(p + \frac{\sqrt{\pi}\hbar}{a}\right)^2}{2m}$
 (c) $\frac{\left(-p + \frac{\sqrt{\pi}\hbar}{a}\right)^2}{2m}$
 (d) $\frac{p^2}{2m} + \frac{\hbar^2}{4a^2m} + \frac{p\hbar}{2ma}$

Solid State Physics**Q47.** [TIFR_2024_A_Q25]

Year 2024 · Solid State Physics · Lattice Vibrations and Thermal Properties · Both int. phd and phd · 3 marks

TIFR GS	2024	Section A
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A student designed a new semiconductor with lattice constant a that crystallizes in the face-centered cubic (fcc) structure. The conduction band minimum of this semiconductor lies at all momentum points equivalent to $\vec{k} = (0.5, 0, 0)\pi/a$. How many conduction band minimum points are inside the first Brillouin zone?

- (a) 6
 (b) 4
 (c) 3
 (d) 1

Q48. [TIFR_2024_B_Q15]

Year 2024 · Solid State Physics · Lattice Vibrations and Thermal Properties · Only int. Phd · 5 marks

TIFR GS	2024	Section B
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The energy dispersion in the conduction band of a one-dimensional metal with lattice spacing a is given by,

$$E(k) = E_0(1 - \cos ka)$$

where $k \in (-\pi/a, +\pi/a]$. Suppose that each site contributes one conduction electron to the conduction band. What is the Fermi energy of the system?

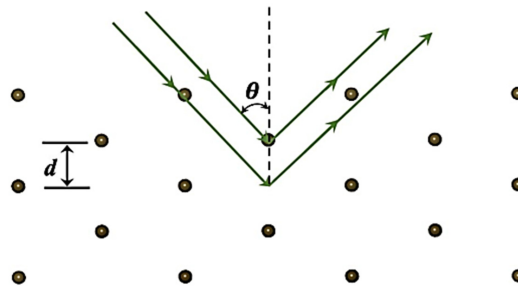
- (a) E_0
- (b) $\frac{E_0}{2}$
- (c) $2E_0$
- (d) $\frac{E_0}{4}$

Q49. [TIFR_2024_C_Q14]

Year 2024 · Solid State Physics · XRay Diffraction · Only PhD · 5 marks

TIFR GS	2024	Section C
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An X-ray of wavelength 3.1\AA is incident on the (110) plane of a cubic lattice with lattice constant a and produces a second-order Bragg reflection at $\theta = 30^\circ$ (θ is the angle measured from normal to the plane as shown in the figure).



What is the value of a ?

- (a) 5.06\AA
- (b) 8.77\AA
- (c) 3.58\AA
- (d) 5.46\AA

Statistical Mechanics

Q50. [TIFR_2024_A_Q14]

Year 2024 · Statistical Mechanics · Microstates · Both int. phd and phd · 3 marks

TIFR GS	2024	Section A
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A string has 8 beads in a row, with n identical red beads and $(8 - n)$ identical blue beads. When one of the red beads is replaced by a blue one, the entropy of the given system changes from S to $S + k_B \ln 2$. All configurations of the beads are equally probable. What is the value of n ?

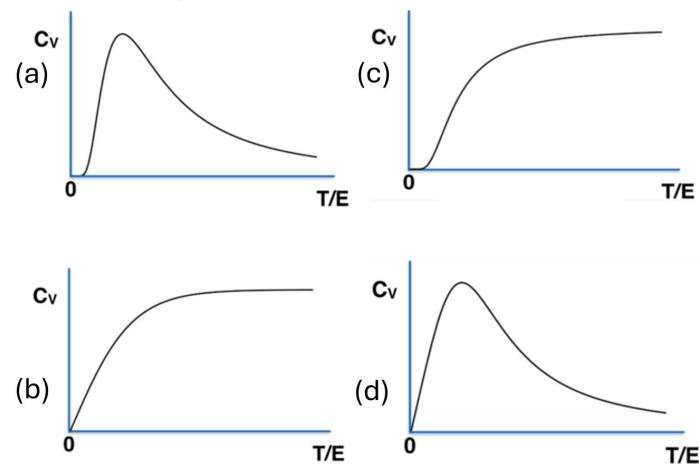
- (a) 6
- (b) 2
- (c) 4
- (d) 8

Q51. [TIFR_2024_B_Q8]

Year 2024 · Statistical Mechanics · Canonical Ensemble · Only int. Phd · 5 marks

TIFR GS	2024	Section B
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A collection of N spin- $1/2$ objects, with individual energy eigenvalues $0, E$ are kept at a temperature T . Which of the following curves accurately represent the temperature dependence of specific heat of the system?

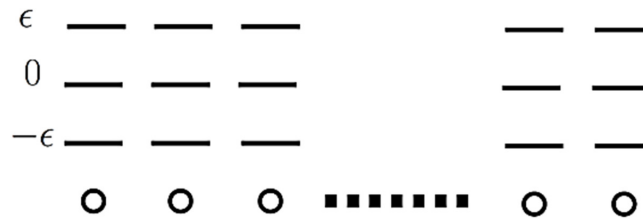


Q52. [TIFR_2024_C_Q8]

Year 2024 · Statistical Mechanics · Microstates · Only PhD · 5 marks

TIFR GS	2024	Section C
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Each site of a linear chain of N sites has a spin which can be in three different states with energies $0, \pm\epsilon$, as shown in the figure below.



The system has a constraint that the neighbouring spins cannot be in the same state. At infinite temperature, the entropy of the system is given by:

- (a) $N \ln 2 + \ln \frac{3}{2}$
- (b) $N \ln 3$
- (c) $(N - 1) \ln 2$
- (d) $N \ln 2$

Thermodynamics**Q53.** [TIFR_2024_A_Q13]

Year 2024 · Thermodynamics · Laws of thermodynamics · Both int. phd and phd · 3 marks

TIFR GS	2024	Section A
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A mass of M kg of water at temperature T_a is isobarically and adiabatically mixed with an equal mass of water at temperature T_b . The specific heat of water at constant pressure is C_p . What is the entropy change (ΔS) of the system?

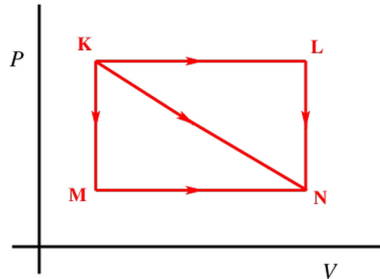
- (a) $\Delta S = MC_p \ln \left\{ 1 + \frac{(T_a - T_b)^2}{4T_a T_b} \right\}$
- (b) $\Delta S = MC_p \ln \left\{ 1 - \frac{(T_a + T_b)^2}{4T_a T_b} \right\}$
- (c) $\Delta S = MC_p \ln \left\{ 1 + \frac{4T_a T_b}{(T_a - T_b)^2} \right\}$
- (d) $\Delta S = MC_p \ln \left\{ \frac{T_a + T_b}{\sqrt{T_a T_b}} \right\}$

Q54. [TIFR_2024_A_Q15]

Year 2024 · Thermodynamics · Laws of thermodynamics · Both int. phd and phd · 3 marks

TIFR GS	2024	Section A
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An ideal gas on the Pressure (P)-Volume (V) diagram can be taken from point K to point N along three different paths, as shown below. $K \rightarrow L \rightarrow N$, $K \rightarrow M \rightarrow N$, and $K \rightarrow N$.



Which of the following options is a true statement?

- (a) The change in internal energy is the same along each path
- (b) The same work is done along each path
- (c) The same amount of heat is added to each the gas along each path
- (d) There is no work done along the path $K \rightarrow N$

Q55. [TIFR_2024_B_Q9]

Year 2024 · Thermodynamics · Carnot Cycle · Only int. Phd · 5 marks

TIFR GS	2024	Section B
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An ideal heat pump delivers heat at a rate $\beta(T_H - T_S)$ from the colder surroundings (S) at a temperature T_S to a heater (H) kept at a constant temperature T_H . Here β is a constant. What is the power consumption of the heat pump?

- (a) $\frac{\beta(T_H - T_S)^2}{T_H}$
- (b) $\beta(T_H - T_S)$
- (c) $\frac{\beta(T_H - T_S)^2}{T_S}$
- (d) $\frac{\beta(T_H - T_S)T_H}{T_S}$

Answer Key & Index

Complete TIFR GS Physics Paper · 2024 · 55 questions

#	Question ID	Subject	Topic	Ans	Marks
1	TIFR_2024_C_Q11	Atomic and Molecular Physics	Effects in atomic physics	A	5
2	TIFR_2024_A_Q12	Classical Mechanics	Central Forces, Gravitation an	A	3
3	TIFR_2024_A_Q22	Classical Mechanics	Special Theory of Relativity	A	3
4	TIFR_2024_A_Q4	Classical Mechanics	Oscillations	A	3
5	TIFR_2024_A_Q5	Classical Mechanics	Basic Mechanics	A	3
6	TIFR_2024_A_Q6	Classical Mechanics	Basic Mechanics	A	3
7	TIFR_2024_B_Q12	Classical Mechanics	Central Forces, Gravitation an	A	5
8	TIFR_2024_B_Q14	Classical Mechanics	Special Theory of Relativity	A	5
9	TIFR_2024_B_Q2	Classical Mechanics	Central Forces, Gravitation an	A	5
10	TIFR_2024_B_Q3	Classical Mechanics	Lagrangian and Hamiltonian	A	5
11	TIFR_2024_C_Q13	Classical Mechanics	Central Forces, Gravitation an	A	5
12	TIFR_2024_C_Q3	Classical Mechanics	Rotational Motion	A	5
13	TIFR_2024_C_Q4	Classical Mechanics	Lagrangian and Hamiltonian	A	5
14	TIFR_2024_A_Q10	Electromagnetism	Electrostatics	A	3
15	TIFR_2024_A_Q11	Electromagnetism	Multipole Expansion	A	3
16	TIFR_2024_B_Q6	Electromagnetism	Electrodynamics	A	5
17	TIFR_2024_B_Q7	Electromagnetism	Electrostatics	A	5
18	TIFR_2024_C_Q7	Electromagnetism	EM Waves	A	5
19	TIFR_2024_A_Q16	Electronics	Logic Gates	A	3
20	TIFR_2024_A_Q17	Electronics	Logic Gates	A	3
21	TIFR_2024_B_Q10	Electronics	OPAMP	A	5
22	TIFR_2024_A_Q18	Experimental Physics	Data Analysis	A	3
23	TIFR_2024_B_Q11	Experimental Physics	Instruments	A	5
24	TIFR_2024_C_Q10	Experimental Physics	Data Analysis	A	5
25	TIFR_2024_C_Q9	Experimental Physics	Instruments	A	5
26	TIFR_2024_A_Q1	Geometry	Geometry	A	3
27	TIFR_2024_A_Q2	Mathematical Physics	Vector Analysis	A	3
28	TIFR_2024_A_Q3	Mathematical Physics	Differential Equations	A	3
29	TIFR_2024_B_Q1	Mathematical Physics	Limits, Continuity and Differe	A	5
30	TIFR_2024_C_Q1	Mathematical Physics	Matrices	A	5
31	TIFR_2024_C_Q2	Mathematical Physics	Fourier and Laplace Analysis	A	5
32	TIFR_2024_A_Q23	Modern Physics	Light Matter interaction	A	3
33	TIFR_2024_A_Q21	Nuclear and Particle Physics	Radioactivity	A	3
34	TIFR_2024_C_Q12	Nuclear and Particle Physics	Shell Model	A	5
35	TIFR_2024_C_Q15	Nuclear and Particle Physics	Radioactivity	A	5
36	TIFR_2024_A_Q19	Optics	Polarization	A	3

#	Question ID	Subject	Topic	Ans	Marks
37	TIFR_2024_A_Q20	Optics	Interference	A	3
38	TIFR_2024_B_Q13	Optics	Polarization	A	5
39	TIFR_2024_A_Q24	Quantum Mechanics	Potential Well	A	3
40	TIFR_2024_A_Q7	Quantum Mechanics	quantum Harmonic Oscillator	A	3
41	TIFR_2024_A_Q8	Quantum Mechanics	quantum Harmonic Oscillator	A	3
42	TIFR_2024_A_Q9	Quantum Mechanics	Angular Momentum and Hydrogen	A	3
43	TIFR_2024_B_Q4	Quantum Mechanics	Basic Quantum Mechanics	A	5
44	TIFR_2024_B_Q5	Quantum Mechanics	Basic Quantum Mechanics	A	5
45	TIFR_2024_C_Q5	Quantum Mechanics	Basic Quantum Mechanics	B	5
46	TIFR_2024_C_Q6	Quantum Mechanics	Basic Quantum Mechanics	A	5
47	TIFR_2024_A_Q25	Solid State Physics	Lattice Vibrations and Thermal	A	3
48	TIFR_2024_B_Q15	Solid State Physics	Lattice Vibrations and Thermal	A	5
49	TIFR_2024_C_Q14	Solid State Physics	XRay Diffraction	A	5
50	TIFR_2024_A_Q14	Statistical Mechanics	Microstates	A	3
51	TIFR_2024_B_Q8	Statistical Mechanics	Canonical Ensemble	A	5
52	TIFR_2024_C_Q8	Statistical Mechanics	Microstates	A	5
53	TIFR_2024_A_Q13	Thermodynamics	Laws of thermodynamics	A	3
54	TIFR_2024_A_Q15	Thermodynamics	Laws of thermodynamics	A	3
55	TIFR_2024_B_Q9	Thermodynamics	Carnot Cycle	A	5

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